# PREDICTIVE ABILITY OF THE STRIPED BASS MODEL 

July 27, 1992

The purpose of this exhibit is to investigate the ability of the Striped Bass Model ("Model") to predict the number of adult bass in the Sacramento-San Joaquin Estuary ("Estuary") that would result from a given level of Delta outflow and exports. The Model is summarized from WRINT-DFG-Exhibit 3 in Figure 1.1 The raw data that the California Department of Fish and Game ("CDFG") reportedly used to develop the Model is presented in Appendix A. ${ }^{2}$

## 1. VALIDATION

Several reviewers pointed out the need to validate the Model using data that had not been used to develop the Model, including the Department of Water Resources ("DWR"), Hanson, and Jones \& Stokes. ${ }^{3}$ Regression models are normally validated by comparing predictions to actual values that were not used to develop the model. This can be achieved by collecting fresh data or by
${ }^{1}$ David W. Kohlhorst, Donald E. Stevens, and Lee W. Miller, A Model for Evaluating the Impacts of Freshwater Outflow and Export on Striped Bass in the Sacramento-San Joaquin Estuary, WRINT-DFG-Exhibit 3, July 1992.

2 CDFG's regression equations were checked using the data in Appendix A. All of the equations shown in Figure 1 can be duplicated except those that are based on April through July flows. The equations obtained using the data in Appendix $A$ are:
(2) Residual YOY $=1 /[0.00995+(2.41 / E g g s)]-60$
(3) Suisun Index $=46.61$ Log (Mean Apr-Jul Outflow) - 158.86
(4) Delta Index $=288.827$ Log (Mean Apr-Jul Outflow)

- 34.445 (Log (Mean Apr-Jul Outflow)) ${ }^{2}$
- 0.00560 (Mean Apr-July Diversions)
- 527.400

We suspect that CDFG estimated the above three equations using an early version of DAYFLOW. We used CDFG's data from Appendix A and our refit of Equations 2 through 4 in this footnote in all of the analyses reported herein.

3 Letter from Edward F. Huntley, DWR, to D. Beringer, SWRCB, November 1, 1992, p. 2, Comment 3; Letter from Charles W. Hanson, Hanson Environmental, to David W. Kohlhorst, CDFG, November 7, 1991, p. 1; Letter from W.J. Shaul, Jones \& Stokes, November 1, 1992, p. 1-2.

Figure 1.
DFG STRIPED BASS MODEL

## (WRINT - DFG - Exhibit 3)

2 Residual $\mathrm{YOY}=[1 /(0.0095+(2.59 /$ Eggs $))]-60 \quad$ (p. 27)

3 Suisun Index $=46.680$ Log(Mean Apr-Jul Outflow) - 159.077
(p. 27)

5 YOY Index = Residual YOY + Suisun Index + Delta Index


6 Log(Loss Rate) $=0.00013593$ (Mean Aug-Mar Exports) 0.00001553 (Mean Aug-Dec Outflow) +4.6226
(p. 35)

- When applying Equation 7, multiply Mean YOY and Mean Loss Rate by 0.4238
${ }^{* *} x=1.08$ when adults in Equation $1=1.7$ million; $x=0.936$ when adults in Equation $1=1$ million
splitting the data set and using part to fit the model and the rest to validate it.

The CDFG did not validate the version of the Model included in WRINT-DFG-Exhibit 3 and has not adequately validated any version of the Model. Figure 6 in WRINT-DFG-Exhibit 3 is not a validation. Rather, it shows how well one of the six regression equations fits the measured data, not how well the Model will predict future values. The predicted values in CDFG's Figure 6 were apparently estimated using the Adult equation (Eq. 7, Fig. 1) alone with data used to develop the Model in the first place. CDFG also apparently applied the Model in the same way that it was developed, while in practice, the Model is applied very differently. ${ }^{4}$

Basic textbooks on regression ${ }^{5}$ routinely recommend validation to assess the predictive accuracy of regression models. For example, Drs. Montgomery and Peck in Introduction to Linear Regression Analysis ${ }^{6}$ point out that:

There is no assurance that the equation that provides the best fit to existing data will be a successful predictor. Influential factors that were unknown during the model-building stage may significantly affect the new observations, rendering the predictions almost useless. Furthermore the correlative structure between the regressors may differ in the model-building

4 In developing the Model, the mean Yoy index and loss rate 3 to 7 years earlier are used, while in applying the Model, point estimates of the YOY index and loss rate are used. Similarly, in developing the Model, individual weighting factors for each year are used, while in applying the Model, the mean annual weighting factor of 0.4238 is used. Finally, when applying the Model, adult abundance is multiplied by 1.08 when adults in Equation 1 average 1.7 million (prior to 1976) and by 0.936 when adults in Equation 1 average 1.0 million (after 1976) [WRINT-DFG-Exhibit 3, p. 39]. This introduces significant uncertainty into the predicted results, as discussed in Section 3.3.
${ }^{5}$ See, for example, Dick R. Wittink, The Application of Regression Analysis, Allyn and Bacon, Inc., Boston, 1988, Chapter 10; Douglas C. Montgomery and Elizabeth A. Peck, Introduction to Linear Regression Analysis, 2nd Edition, John Wiley \& Sons, Inc., New York, 1991, Chapter 10; Norman Draper and Harry Smith, Applied Regression Analysis, 2nd Edition, John Wiley \& Sons, New York, 1981, p. 419-422.

6 D.C. Montgomery and E.A. Peck, Introduction to Linear Regression Analysis, 2nd Edition, John Wiley \& Sons, Inc., New York, 1992, p. 443.
and prediction data. This may result in poor predictive performance for the model. Proper validation of a model developed to predict new observations should involve testing the model in that environment before it is released to the user.

Dr. Wittink, in The Application of Regression Analysis ${ }^{7}$, likewise writes:

> The validity of the final model is usually assessed in terms of predictive accuracy. That is, the estimated equation (from the estimation sample) is used to predict values for the criterion variable in the validation samples. These predicted values are then compared with the actual values. Note that in this case the observations in the validation sample are not used to estimate parameters. Instead, the parameters estimated in the estimation sample are used to obtain the predicted values in the validation sample.

We evaluated the predictive ability of the Model by eliminating 1987 through 1991 from the data sets, refitting the equations, and using the refitted equations to predict adult abundance. The same form of the equations shown in Figure 1 was refit to the shorter data sets. The predictions are based on point estimates rather than 3 to 7 year backaverages and annual weighting to accurately reflect the way the Model is actually applied.

The results of this analysis are shown in Table 1. In three out of the four years, predicted adult abundance is about half of actual abundance, while in one year, predicted abundance is about 20 percent higher than actual. Thus, the predictive ability of the Model is poor.
2. CONFIDENCE INTERVALS

The predictive ability of a regression model is normally evaluated using 95 percent confidence intervals. A confidence interval is a measure of the uncertainty associated with a model. The 95 percent confidence interval, for example, means that there is a 95 percent probability that the true value lies between the upper and lower limits. Although regression equations and their coefficients may be statistically significant (i.e., p<0.05), the equations can have wide confidence intervals due to statistical

[^0]TABLE 1. VALIDATION OF STRIPED BASS MODEL FOR 1987-1990
Data Used for Model Valldation

| Year | Adults ${ }^{2}$ (inc. hatchery fish) | Aug-Mar Exports | Aug-Dec Outflow | $\begin{aligned} & \text { Log } \\ & \text { Apr-Jul } \\ & \text { Outtlow } \\ & \hline \end{aligned}$ | Log Apraul Outflow ${ }^{2}$ | Apr-Jul Diversions | Weighting Factor |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1987 | 1.076649039 | 8,513 | 4.435 | 3.6667 | 13.4446 | 9,721 | 0.4238 |  |
| 1988 | 0.960533285 | 8,059 | 4,402 | 3.7665 | 14.1863 | 10,278 | 0.4238 |  |
| 1989 | 0.831278945 | 10,644 | 5,208 | 3.9033 | 15.2355 | 10,967 | 0.4238 |  |
| 1990 | 0.461551749 | 5,550 | 4,337 | 3.7595 | 14.1340 | 8,802 | 0.4238 |  |
| Refifted Equations |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Predicted | Actual |
| 1. Eggs $=96.94(\text { Adults })^{2}+25.33$ |  |  |  |  |  | 1987 | 129.7 | 176.0 |
|  |  |  |  |  |  | 1988 | 118.4 | 176.4 |
|  |  |  |  |  |  | 1989 | 105.9 | 103.5 |
|  |  |  |  |  |  | 1990 | 70.1 | 91.6 |
| 2. Correction Factor $=[1 /(0.0107+(2.14 / E g g s)]$-60 |  |  |  |  |  | 1987 | -23.2 | -13.5 |
|  |  |  |  |  |  | 1988 | -25.2 | -26.3 |
|  |  |  |  |  |  | 1989 | -27.6 | -31.8 |
|  |  |  |  |  |  | 1990 | -35.8 | -34.4 |
| 3. Suisun Index $=46.61$ Log(A-J Outflow)-158.86 |  |  |  |  |  | 1987 | 12.0 | 5.3 |
|  |  |  |  |  |  | 1988 | 16.7 | 0.7 |
|  |  |  |  |  |  | 1989 | 23.1 | 2.0 |
|  |  |  |  |  |  | 1990 | 16.4 | 1.5 |
| 4. Delta Index $=288.827 . \log (A-J \text { Outflow)-34.445(Log(A-J Outflow) })^{2}$$0.00560($ A-J Diversions)-527.4000 |  |  |  |  |  | 1987 | 14.1 | 7.3 |
|  |  |  |  |  |  | 1988 | 14.3 | 3.9 |
|  |  |  |  |  |  | 1989 | 13.8 | 3.1 |
|  |  |  |  |  |  | 1990 | 22.3 | 2.8 |
| 5. YOY Index = Correction Factor+Suisun Index+Delta Index |  |  |  |  |  | 1987 | 2.9 | 12.6 |
|  |  |  |  |  |  | 1988 | 5.7 | 4.6 |
|  |  |  |  |  |  | 1989 | 9.2 | 5.1 |
|  |  |  |  |  |  | 1990 | 2.9 | 4.3 |
| 6. Log Loss Rate $=\mathbf{0 . 0 0 0 1 2 4 7 6 ( A - M ~ E x p o r t s ) - 0 . 0 0 0 0 1 4 4 5 ( A - D ~ O u t f l o w ) ~}+$ 4.6373 |  |  |  |  |  | 1987 | 5.6353 | 6.0467 |
|  |  |  |  |  |  | 1988 | 5.5791 | 5.6271 |
|  |  |  |  |  |  | 1989 | 5.8900 | 6.0772 |
|  |  |  |  |  |  | 1990 | 5.2671 |  |
| 7. Adults $=0.936[20336$ WMYOY-486819 Log(WMLossRate) +3112988 ] |  |  |  |  |  | 1987 | 539,342 | 998,349 |
|  |  |  |  |  |  | 1988 | 587,505 | 903,899 |
|  |  |  |  |  |  | 1989 | 473,985 | 786,380 |
|  |  |  |  |  |  | 1990 | 707,311 | 591,241 |

and structural defects, reducing one's certainty about the magnitude of the predicted value. ${ }^{8}$

Three types of confidence intervals are commonly used in regression analysis. These are confidence intervals on the conditional mean, ${ }^{9}$ predicted values, and fitted coefficients.

### 2.1. CDFG's Confidence Intervals

In WRINT-DFG Exhibit 3, CDFG estimated 95 percent confidence intervals for the Adult equation (Eq. 7, Fig. 1) and reported them in Figure 6 of WRINT-DFG-Exhibit 3. The CDFG confidence intervals are a very narrow band, implying a high degree of confidence in the Model's predictions. Although CDFG did not explain how they estimated their confidence intervals, backcalculation indicates that CDFG's confidence intervals are estimated for the conditional mean for only the Adult equation (Eq. 7, Fig. 1). CDFG's confidence intervals are not relevant for estimating how well the Model predicts because they are on the conditional mean not the predicted value, and they are for one equation only, rather than the set of seven equations that comprise the Model.
2.1.1 Prediction Intervals. Prediction confidence intervals must be used to determine the uncertainty in predicted values. The conditional mean confidence intervals that CDFG used are for the regression line itself, not individual predicted values. Prediction confidence intervals for each of the six regression equations are shown in Figure 2. Prediction intervals for the Model as a whole must include the uncertainity in each of these six equations as well as the uncertainity associated with substituting each result into subsquent equations.

Figure $2 f$ shows confidence intervals on predicted values superimposed over confidence intervals on the conditional mean for the Adult equation. Note that 35 percent or eight out of 23 of the observed values for adult abundance, fall outside of the conditional mean intervals of CDFG's Figure 6. The reason that so many points fall outside of the band is that the conditional mean confidence intervals are not designed to encompass predicted values, only the regression line. The uncertainty in individual predictions is always greater than the uncertainty in the
${ }^{8}$ Wittink, 1988, p. 39.
9 The "conditional mean" is the average predicted value of $y$ based on the condition of a specific value of $X$. The conditional mean, for example, might be the average Suisun yoy Index for all years when the April to July Delta outflow was equal to 5,000 cfs. Confidence intervals on the "conditional mean" are the same thing as confidence intervals for the regression line.

Figure 2. $95 \%$ Confidence Intervals for the Predicted Values

(c) Log(Loss Rate) $=0.00013593$ (Mean Aug-Mar Exports)-


Year

- Actual Value - Predicted Value - - Confidence Intervals

Figure 2 (Continued). 95\% Confidence Intervals for the Predicted Values

(e) Delta Index $=288.827 \mathrm{Log}$ (Mean Apr-Jul Outflow)-34.445(Log(Mean

(f) Adults $=18940$ Weighted Mean YOY-446608Log(Weighted
 Mean Loss Rate)+2960840

conditional mean. ${ }^{10}$ The predicted value interval is the appropriate interval to assess predictive ability.
2.1.2 Model Intervals. The second problem with CDFG's confidence intervals is that they are for only the Adult equation, not the six regression equations that comprise the Model (Eqs. 1-4, 6, 7, Fig. 1). Each of these six equations also has 95 percent confidence intervals, as shown in Figure 2. Therefore, to determine 95 percent confidence intervals for predictions made with the Striped Bass Model, confidence intervals that combine the error in all six equations and simultaneously apply to all six regression equations must be constructed.

CDFG's confidence intervals only apply when the Adult equation (Eq. 7, Fig. 1) is used in isolation to predict the conditional mean. In other words, the CDFG intervals apply only when a measured YOY (rather than one estimated from Eqs. 1 - 5 in Fig. 1) and a measured loss rate (rather than one estimated from Eq. 6) is used to estimate conditional mean adults. This is not how the Model is applied. The Model is applied by using hydrologic variables to estimate the Suisun and Delta indices and the loss rate, which are then plugged into the Adult equation. Thus, the uncertainty in each of the six regression equations must be combined to determine the total uncertainty of the Model.

In sum, CDFG's confidence intervals give the misleading -impression that the Model is a precise predictor of adult abundance. As shown below, the Model does not accurately predict adult abundance.
2.2. Confidence Intervals For The Model

The most straightforward way to estimate confidence intervals ${ }^{11}$ for the Model would be to combine the seven equations into a single equation and use the raw data (Appx. A) in the usual way to compute confidence intervals. When this is attempted with the Striped Bass Model, it reduces to an equation ${ }^{12}$ of the form:

10 Wittink, 1988, p. 47.
${ }^{11}$ Henceforth, when the term "confidence intervals" is used, it refers to confidence intervals on the predicted value unless otherwise stated.

12 The actual equation reduces to:

$$
\begin{aligned}
\text { Adults }_{0}= & {\left[a W / A^{2 d u l t s}{ }_{h}^{2}+b W L O g(A J O)+c W\left(\log (A J O)^{2}\right.\right.} \\
& +d W(A J D)+e L O g(W X A M E)+f \log (\text { WXADO })]_{\text {lagged } 3-7 \mathrm{yrs}}
\end{aligned}
$$

Adults (without hatchery fish) $=$ a function of
[1/Adults ${ }^{2}$ (with hatchery fish) + Outflow + Diversions]lag
Notice that "adults" is a response variable (Y) and that the reciprocal of lagged adults ${ }^{2}$ is one of the predictor variables (X's). The Model, in effect, predicts adults from one over the square of 3 to 7 year lagged adults ${ }^{12}$.

We fit this single equation to the data, and the results are shown in Table 2. Examining the probabilities (p), it is obvious that neither the Model as a whole ( $p=0.07$ ) nor the individual fitted coefficients ( $p=0.14$ to 0.75 ) with the exceptions of August to December outflow, are significant at the 5 percent level. The $p$ values shown in Table 2 are understated due to violations of the underlying assumptions of regression analysis, including the requirement that the predictor variables are independent and that the residuals have equal variance. ${ }^{13}$

Examining the signs on the various fitted coefficients, intuitively, it appears the Model is not correct. The fitted Model predicts that adult abundance: (1) decreases when adults 3 to 7 years earlier increase; (2) increases when August to March exports increase; and (3) decreases when the square of April to July outflow increases. These results raise significant questions about the validity of the seven-equation Model that the single equation model was derived from.

Clearly, the single-equation model is not useful for prediction because 5 of the 6 fitted constants are not statistically significant and have inconsistent signs. Further, the Model as a whole is not statistically significant at the 5 percent level ( $\mathrm{r}^{2}=0.45, \mathrm{p}=0.07$ ). This is in part due to extreme collinearity and other statistical defects, as discussed in Section 3. Since the single-equation model is useless for prediction, confidence limits have no meaning and are not calculated.
2.2.1 Prediction Error. Because confidence intervals are not strictly defined for the Model, confidence intervals on the
where the subscript o indicates adults without hatchery fish, the subscript $h$ indicates adults with hatchery fish, $W$ is a weighting factor, AJO is the April to July outflow, AJD is the April to July diversions, AME is the August to March exports, ADO is the August to December outflow, and "a" through "f" are regression coefficients.
${ }^{13}$ Rupert G. Miller, Jr., Beyond ANOVA. Basics of Applied Statistics, John Wiley \& Sons, New York, 1986, Chapter 5.

TABLE 2. LINEAR LEAST SQUARES REGRESSION FOR AN EQUATION OF THE FORM:.

$$
\begin{aligned}
& \text { Adults[o] }=\left[\text { aW/Adults[h] }{ }^{2}+\text { bWLog(AJO) }+\mathrm{cW}(\log (\text { AJO }))^{2}+\mathrm{dW}(\text { AJD }) ~+\right. \\
& \text { eLog(WxAME) + fLog(WXADO)] [lagged 3-7 years] }
\end{aligned}
$$

where [o] indicates adults without hatchery fish, [h] indicates aduts with hatchery fish, W is a weighting factor,
AJO is April to July outtlow, AJD is April to July diversions, AME is August to March exports, ADO is
August to December outflow, and a through $f$ are regression coefficients

| Year | Adults[0] | Lag 1/Wght Adults[h] ${ }^{2}$ | $\begin{aligned} & \text { Lag Wght } \\ & \text { Log AJO } \end{aligned}$ | Lag Wght <br> $\log \mathrm{AJO}^{2}$ | $\begin{gathered} \text { Lag Wght } \\ \text { AJD } \\ \hline \end{gathered}$ | Lag Wght Log AME | Lag Wght Log ADO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1969 | 1,646,026 |  | 0.7399 | 3.0615 | 1188.80 | 1.2034 | 1.6707 |
| 1970 | 1,727,394 |  | 0.7945 | 3.5411 | 1061.82 | 1.2321 | 1.6473 |
| 1971 | 1,599,715 |  | 0.7414 | 3.0943 | 1259.43 | 1.3189 | 1.6006 |
| 1972 | 1,882,907 |  | 0.7875 | 3.4853 | 1179.44 | 1.2926 | 1.6405 |
| 1973 | 1,637,159 |  | 0.7492 | 3.1529 | 1285.55 | 1.3037 | 1.6878 |
| 1974 | 1,477,213 |  | 0.7668 | 3.2903 | 1395.37 | 1.3351 | 1.6657 |
| 1975 | 1,849,770 |  | 0.7199 | 2.9051 | 1566.62 | 1.3494 | 1.6470 |
| 1976 | 1,581,076 | 0.347332 | 0.7233 | 2.9230 | 1626.36 | 1.3802 | 1.7004 |
| 1977 | 924,301 | 0.399867 | 0.7698 | 3.3193 | 1794.81 | 1.4025 | 1.6904 |
| 1978 | 1,151,642 | 0.353697 | 0.7826 | 3.4199 | 1682.04 | 1.4501 | 1.6554 |
| 1979 | 1,155,701 | 0.372179 | 0.7293 | 2.9851 | 1546.41 | 1.4388 | 1.5164 |
| 1980 | 1,115,999 | 0.750805 | 0.6800 | 2.5990 | 1191.19 | 1.4241 | 1.4369 |
| 1981 | 911,300 | 0.779775 | 0.7334 | 3.0294 | 1333.48 | 1.4243 | 1.4690 |
| 1982 | 825,126 | 0.772918 | 0.7267 | 2.9590 | 1553.29 | 1.4471 | 1.4966 |
| 1983 | 1,009,748 | 0.790352 | 0.7456 | 3.1065 | 1583.91 | 1.4608 | 1.4980 |
| 1984 | 1,042,668 | 0.994026 | 0.7246 | 2.9321 | 1603.01 | 1.4690 | 1.6051 |
| 1985 | 1,024,188 | 1.225278 | 0.7893 | 3.4974 | 1621.51 | 1.4758 | 1.6987 |
| 1986 | 1,037,127 | 1.131474 | 0.8364 | 3.9219 | 1488.16 | 1.4268 | 1.7913 |
| 1987 | 998,349 | 1.031355 | 0.7897 | 3.5039 | 1655.50 | 1.4492 | 1.7317 |
| 1988 | 903,899 | 0.990185 | 0.7350 | 3.0397 | 1773.63 | 1.4730 | 1.5808 |
| 1989 | 786,380 | 0.957085 | 0.7495 | 3.1462 | 1704.97 | 1.4815 | 1.5358 |
| 1990 | 591,241 | 0.969013 | 0.7059 | 2.7939 | 1719.77 | 1.4939 | 1.4598 |
| 1991 | 961,063 | 1.090548 | 0.6872 | 2.6373 | 1785.90 | 1.4983 | 1.4154 |

Regression Statistics

| Multiple R | 0.817581672 |
| :--- | ---: |
| R Square | 0.668439791 |
| Adjusted R Sq. | 0.447399651 |
| Standard Error | 157089.8694 |
| Observations | 16 |

Anaysis of Variance

|  | A | Sum ol Squares | Mean Square | F | Significance $F$ |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Regression | 6 | $4.47753 \mathrm{E}+11$ | 74625543253 | 3.024065185 | 0.066367446 |
| Residual | 9 | $2.22095 \mathrm{E}+11$ | 24677227072 |  |  |
| Total | 15 | $6.69848 \mathrm{E}+11$ |  |  |  |


| Variable | Coefficients | Slandard Enor | tSabsisic | P-value | Lower 95\% | Uppar 95\% |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Intercept | -5913771.35 | 12361974.46 | -0.4783840 | 0.6392747 | -33878521.72 | 22050979.03 |
| 1/Adults $\left[\right.$ h] ${ }^{2}$ | -277734.89 | 286649.57 | -0.9689004 | 0.3479592 | -926181.77 | 370711.99 |
| Apr-Jul Out | 12429856.98 | 34912934.91 | 0.3560244 | 0.7267800 | -66548749.00 | 91408462.96 |
| Apr-Jul Out | -1995662.99 | 4114756.94 | -0.4850014 | 0.6346820 | -11303896.98 | 7312571.00 |
| Apr-Jul Diversn | -643.95 | 417.60 | -1.5420213 | 0.1438984 | -1588.64 | 300.73 |
| Aug-Mar Exp | 1038084.05 | 3152439.04 | 0.3292955 | 0.7464854 | -6093233.94 | 8169402.03 |
| Aug-Dec Out | 2297247.47 | 939383.29 | 2.4454847 | 0.0272822 | 172213.22 | 4422281.72 |

regression coefficients were used to give an indication of the error in predicted values. Model predictions are no better than the estimated coefficients. The prediction error was computed by first replacing all of the regression coefficients with their upper 95 percent confidence limit and using the Model in the usual way to predict adult abundance. Then, the regression coefficients were replaced with the lower 95 percent limit and adult abundance predicted in the usual way.

The results of this analysis are shown in Figure 3. The intervals shown on Figure 3 are not confidence intervals, but rather a worst-case estimate of the error associated with Model predictions. Additional estimates could be obtained by using different combinations of confidence limits on the coefficients.

Figure 3 shows that errors in the regression coefficients could cause errors of over $+/-2000$ percent in predicted adult abundance. The very wide error band is caused by structural and statistical problems such as multicollinearity, which affect the accuracy of the estimated coefficients. The large prediction error of the Model (Fig. 3) suggests that it is not useful for forecasting adult abundance.
3. FACTORS THAT INFLUENCE THE PREDICTIVE ABILITY OF THE STRIPED BASS MODEL

Many reviewers raised statistical criticisms of the Striped Bass Model, including multicollinearity, autocorrelation, averaging, and propagation of errors, among others. CDFG dismissed these statistical concerns, arguing that as long as the equations make biological sense, statistical flaws are unimportant. For example, in their November 21, 1991 response to comments to the State Water Resources Control Board ("SWRCB"), they state: "[w]e also believe that complete statistical rigor is not essential...Nevertheless, the model makes sense conceptually and biologically and does a good job at predicting abundance within the range of past observations."14

However, when the errors in CDFG's analysis are corrected, one finds that the Model does not do a good job at predicting adult abundance (Secs. 1,2). Further, some of the structural and statistical defects discussed below suggest that the Model may also have biological flaws. Regardless, a model can make biological sense, but not statistical sense, and thus not be able

[^1]
to make accurate predictions. In order to be useful as a management tool, a model must be able to make reasonably accurate predictions. The statistical problems raised by the reviewers are valid concerns that strongly affect the ability of the Model to make accurate predictions. Further, because the interrelationships among variables are not accurately modelled due to multicollinearity and autocorrelation, the Model also is not useful for studying relative changes and differences among alternatives because management options necessarily involve changing the inter-relationships among variables.

The large uncertainty in the Model's predictions are due to statistical flaws, measurement errors, and model specification errors, as discussed below.

### 3.1. Multicollinearity

One of the principal assumptions of regression analysis is that the predictor or explanatory variables (the X's) are independent (i.e., the value of one predictor variable does not depend on the value of any of the other predictor variables). Multicollinearity or simply "collinearity," refers to the situation when the predictor variables are related to each other. Severe collinearity indicates that a substantial part of the information in one or more of the predictor variables is redundant, which makes it difficult to separate the effects of the different predictor variables on the response variable (the Y).

When collinearity is present, the standard errors associated with the regression coefficients are inflated, the coefficients themselves may be unreasonable, and confidence intervals are larger than they otherwise would be. In fact, the coefficient of determination ( $\mathrm{r}^{2}$ ) can be high and the regression equation can be statistically significant while the individual fitted parameters are not statistically significant and the prediction intervals are large. ${ }^{15}$ Chatterjee and Price warned that "one should be extremely cautious about any and all substantive conclusions based on a regression analysis in the presence of multicollinearity" ${ }^{16}$ and that multicollinearity "...can seriously limit the use of regression analysis for inference and forecasting. Extreme care is required when attempting to

[^2]interpret regression results when multicollinearity is suspected. 117

The six individual regression equations were tested for the presence of collinearity using principal component analysis. The analyses indicate that collinearity is a severe problem for the Delta Index equation (Eq. 4, Fig. 1) and for the Adult equation (Eq. 7, Fig. 1) and is also present to a lesser extent in the Loss Rate equation (Eq. 6, Fig. 1). This indicates that the regression coefficients in these equations may have been degraded and that confidence intervals and predictions could be improved by using better conditioned data. ${ }^{18}$ Collinearity appears to be one of the reasons that the error in predicted values (Fig. 3) is so large.

In the Adult equation, collinearity is present because the yoy index and loss rate are correlated with each other $\mathrm{r}^{2}=$ $0.79, \mathrm{p}<0.01$ ). Most reviewers ${ }^{19}$ correctly noted that in the Adult equation, the YOY index is correlated with loss rate because loss rate is the ratio of export losses to the YOY index. When the log loss rate equation is refitted using export losses rather than loss rate, the $r^{2}$ drops from 0.77 to 0.17 , demonstrating that August to March exports and outflow explain very little of the variability in export losses. In contrast, replacing loss rate with export losses in the Adult equation does not significantly affect the $r^{2}$, indicating that adult abundance

17 Chatterjee and Price, 1991, p. 184.
18 David A. Belsley, Edwin Kuh, and Roy E. Welsch, Regression Diagnostics: Identifying Influential Data and Sources of Collinearity, John Wiley \& Sons, New York, 1980, Chapter 3.

19 Letter from Warren J. Shaul, Jones \& Stokes, to Pete Chadwick, CDFG, Re: Comments on California Department of Fish and Game's Proposed Striped Bass Impact Methodologies for the BayDelta Water Right Environmental Impact Report (EIR), November 1, 1992, pp. 3-4; Letter from Roger K. Patterson, Bureau of Reclamation, to Pete Chadwick, CDFG, Re: Comments on Draft Striped Bass Paper of Department of Fish and Game, Presented at State Water Resources Control Board Workshop on October 25, 1991 (Bay-Delta Hearings) (Water Rights), November 18, 1991, p. 2, Comment 5a; Letter from Bruce K. Orr, EA Engineering, Science, and Technology, to William Johnston, MID, Re: Comments on the CDFG report by Kohlhorst, Stevens, and Miller, November 1, 1991, p. 3; Letter from James H. Cowan, Jr., University of South Alabama, to Randy Brown, DWR, Re: Comments on Striped Bass Model, January 28, 1992, p. 1, Comment 3; Joseph G. Loesch, Critique of a Means of Evaluating Impacts of Alternative Outflow and Export Criteria on Striped Bass in the Sacramento-San Joaquin Estuary, December 2, 1991, p. 2.
is not significantly affected by August to March exports and outflow.

In the Delta index equation (Eq. 4, Fig. 1), collinearity is present because April to July outflow and April to July outflow squared are highly correlated ( $r^{2}=0.99, p<0.01$ ). As a result, at the 5 percent significance level, the fitted coefficients for the intercept ( $p=0.27$ ), log April to July outflow ( $p=0.21$ ), and squared log April to July outflow ( $\mathrm{p}=0.20$ ) are not statistically significant, even though the regression equation as a whole is statistically significant ( $p=0.026$ ) . Further, the negative coefficient for squared log April to July outflow is not consistent with the positive coefficient for log April to July outflow. In fitting polynomials, collinearity can be eliminated by centering the measured predictor variables on their mean values before computing the power (e.g., squared) and fitting the equation.

In the loss rate equation, collinearity is present because August to March exports are correlated with August to December outflow. As discussed in Section 3.2 and pointed out by willits, "the predictors that are of central interest (water exports) are correlated with time (they increase over time) so this creates collinearity between exports and time. Moreover, most of the additional predictors that have been suggested also vary with time, and so it's rather difficult to separate between an effect due to water exports and due to other variables that vary similarly... "20

In some cases, collinearity may not adversely affect the ability of a model to predict, so long as the relationship between the predictor variables does not change. For example, if the relationship between YOY index and loss rate remained constant in the future, the mis-specified Model could still be used to make reasonable predictions if there were no other problems. However, if the relationships between these correlated variables change, the Model would not be able to make accurate predictions. For example, if export losses were reduced by structural changes in Clifton Court Forebay, the relationship between loss rate (export losses/yOY index) and yoy index would change, invalidating predictions with the Model. Similarly, if reservoir operations were changed, the relationship between outflow and exports could change.

Because the Model would be used to explore exactly these types of options, it is of questionable utility as a management tool because it does not model the actual inter-relationships among variables. Thus, regardless of whether the Model makes biological since, collinearity is a serious concern because it

[^3]limits the utility of the Model for predicting and for exploring management options.

### 3.2. Autocorrelation

For time series data, autocorrelation or "self-correlation" means that individual values in a time series, such as Delta outflow or exports, are correlated with past or future values in the series. In other words, for example, April Delta outflow may depend on March Delta outflow, and so forth. The presence of autocorrelation in time series data is usually tested by using the first-order autocorrelation coefficient, which is nothing more than the correlation coefficient ( $r$ ) obtained by regressing the time series with the same series shifted by one observation (e.g., $Y_{2}, Y_{1} ; Y_{3}, Y_{2} ; Y_{n} ; Y_{n-1}$ ).

First-order autocorrelation coefficients were estimated for all data sets used to developed the Striped Bass Model. The results, shown in Table 3, indicate that strong autocorrelation is present in all individual time series, except log April to July outflow. Autocorrelation in the response and predictor variables can cause badly misleading results when estimating regression models due to time-lagged relationships, feedback from predictor to response variables, and correlated regression residuals, among others. These problems, which are discussed below, can be corrected by using dynamic regression which takes into account the time-lagged relationships between response and predictor variables. ${ }^{21}$
3.2.1 Time-Lagged Relationships. The response variable $Y_{t}$ may be related to the predictor variable $X_{t}$ with a time lag; that is, $X_{t}$ may be related to $X_{t-1}, X_{t-2}, X_{t-3}$, and so forth, in addition to (or instead of) being related to $x_{\text {t }}$. For example, instead of the usual first order regression equation

$$
\begin{equation*}
Y_{t}=m X+b \tag{2}
\end{equation*}
$$

which is the basis of the Striped Bass Model, the correct relationship may be

$$
\begin{equation*}
Y_{t}=m_{0} X_{t}+m_{1} X_{t-1}+m_{2} X_{t-2}+b \tag{3}
\end{equation*}
$$

where $b$ is a generic constant that would have different values in equations (1) and (2). If equation (3) is the correct formulation, useful information is lost, for example, about the roles of $X_{t-1}$ and $X_{t-2}$ in explaining the change in $Y_{t}$. Thus, the estimate of the residual variance would be larger than necessary, and predictions would likely be less accurate than otherwise.

[^4]TABLE 3. AUTOCORRELATION IN DATA SETS USED TO DEVELOP STRIPED BASS MODELS

| Variable | $n$ | Lag-1 <br> Autocorrelation Coefficient | Standard Error | Bartlett's ${ }^{1}$ $t$ | Student's t $(\alpha=0.05)$ | Stgnificant ${ }^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Adults | 23 | 0.770 | 0.209 | 3.68 | 2.07 | yes |
| Log Apr-Jul Exports | 33 | 0.371 | 0.174 | 2.13 | 2.04 | yes |
| Log Aug-Dec Outtow | 33 | 0.631 | 0.174 | 3.63 | 2.04 | yes |
| Aug-Mar Exports | 32 | 0.758 | 0.174 | 4.36 | 2.04 | yes |
| Delta YOY Index | 31 | 0.776 | 0.180 | 4.31 | 2.04 | yes |
| Eggs | 23 | 0.750 | 0.209 | 3.59 | 2.07 | yes |
| Log Weighted Mean Loss Rate | 23 | 0.731 | 0.209 | 3.50 | 2.07 | yes |
| Log Apr-Jul Outilow | 33 | -0.065 | 0.174 | -0.37 | 2.04 | no |
| Log Loss Rate | 31 | 0.569 | 0.180 | 3.16 | 2.04 | yes |
| Export Losses | 31 | 0.476 | 0.180 | 2.64 | 2.04 | yes |
| Suisun YOY Index | 31 | 0.437 | 0.180 | 2.43 | 2.04 | yes |
| Weighted Mean YOY | 23 | 0.820 | 0.209 | 3.92 | 2.07 | yes |

Bartlett's t is the ratio of the Lag-1 autocorrelation coefficient to the standard error.
${ }^{2}$ If the absolute value of Bartlett's $t$ is greater than Student's t , the Lag- 1 autocorrelation coefficient is statistically significant at the 5 percent level in a two-tailed test. This means that the data set is autocorrelated.

Further, the estimate of the fitted regression coefficients associated with $X_{t}$ will be biased and inconsistent if the excluded variables ( $X_{t-1}$ and $X_{t-2}$ ) are correlated with the included variable $X_{t}$. These consequences of autocorrelation affect the ability of the Model to make accurate predictions and the confidence that one can place in predicted values.

The Adult equation contains time-lagged relationships, which CDFG attempted to address by using the weighted mean YOY index and weighted mean loss rate 3 to 7 years earlier. As pointed out correctly by several reviewers ${ }^{22}$, this is an inaccurate way to model time-lagged relationships because useful information on the correct relationships is lost, reducing the accuracy of predictions. Because time averaging is not used when the Striped Bass Model is applied, inaccuracies are compounded.

Although no tests were performed, it is likely that time lagged relationships also exist in the Suisun index, Delta index, and loss rate equations. All of these equations should be refit using dynamic regression to improve their predictive ability.
3.2.2 Misleading Correlations. As explained by Dr. Pankratz in Forecasting with Dynamic Regression Models, "if there are common elements in the autocorrelation structure of $Y_{t}$ and $X_{t}$, then an ordinary regression equation can show a strong relationship between these variables when, in fact, $X_{t}$ has no real explanatory power. ${ }^{23}$ Several reviewers correctly pointed out that the apparent good correlations for some regression equations in the Striped Bass Model are due to the fact that the predictor variables are related to time in the same way as the response variable.

For example, Jones \& Stokes noted that both YOY, exports, and outflow are related to time in the same way, suggesting that the correlation between exports and the Delta Yoy equation is due to their common relationship to time. ${ }^{24}$ Common time relationships are present in the Suisun Index, Delta Index, Adult, and Loss Rate equations. As a result of these common time relationships, correlation coefficients mistakenly show strong relationships among variables that may not be otherwise related, adversely affecting the ability of the Model to make accurate predictions.

22 Letter from David G. Hankin, Humboldt State University, to Randall L. Brown, DWR, January 7, 1992, p. 2, Comment 1; Hanson, November 7, 1991, p. 4; Willits, March 29, 1992, p. 2.
${ }^{23}$ Pankratz, 1991, p. 12.
24 Shaul, November 1, 1991, p. 3.

The CDFG investigated the effect of common time relationships by detrending adult abundance, weighted mean yoy index, export losses, and loss rate. They found that when the time trend is removed, correlations of adult abundance with weighted mean yoy index and weighted mean loss rate disappear. ${ }^{25}$ This suggest that the good correlation for the Adult equation ( $r^{2}$ $=0.71, p<0.01$ ) is largely due to time trends, as suggested by the reviewers, rather than any fundamental relationship between variables.

The effect of time trends was further explored by regressing adult abundance on time alone. The resulting regression equation ${ }^{26}$ explains more of the variance and has lower $p$ values for the regression as a whole and individual coefficients than the Adult equation. Thus, time alone is a better predictor of adult abundance then loss rate and the YOY index.

Although the CDFG believes that this does not mean that the strong relationships are "...spurious, only that they are mostly due to simultaneous major changes in yoy striped bass abundance, entrainment losses, and loss rate that have occurred over time, " 27 they are incorrect. They have demonstrated that the good correlation obtained for the Adult equation is largely due to common time relationships, rather than to a fundamental relationship between adults and loss rate and YOY index. Even though, theoretically, there may be a biological relationship between adults, the YOY index and loss rate, it is obscured by common time trends and is not modelled correctly. For example, if the time trend associated with Delta outflow shifted relative to the time trend in adults due to, for example, a reduction in export losses in Clifton Court Forebay, the Model would no longer make accurate predictions.

### 3.3. Differences In Development And Application

In developing the Model, the mean YOY index and loss rate 3 to 7 years earlier are used to estimate adult abundance, while in applying the Model, point estimates of the YOY index and loss rate are used. Similarly, in developing the Model, individual

25 CDFG, Exhibit WRINT-DFG-Exhibit 3, Table 11 and p. 21 and 24.
${ }^{26}$ Regressing adult abundance on year yields the following equation:

$$
\text { Adults }=-47,513(\text { Year })+95,285,912
$$

where $r 2=0.74(p<0.01)$ and the fitted coefficients are statistically significant ( $p<0.01$ ).

$$
27 \text { Id., p. } 25 .
$$

weighting factors for each year are used, whereas in applying the Model, the mean annual weighting factor of 0.4238 is used. Finally, in applying the Model, adult abundance is multiplied by 1.08 when adults in Equation 1 average 1.7 million (prior to 1976) and by 0.936 when adults in Equation 1 average 1.0 million (after 1976). ${ }^{28}$ As pointed out by Hanson, 29 developing a model using a five year average and applying it for single years can introduce considerable error into Model predictions.

The effect of differences in Model development and application was tested by repeating the validation shown in Table 1 , using five-year back averages for the YOY index and loss rate. The predictions for the backaveraged case (comparable to Model development) are 949,027 bass in 1987; 681,645 in 1988; 869,404 in 1989; and 637,221 in 1990. On average, the ratio of the actual to predicted adults is 1.05 for the development case and 1.50 for the application case (predicted using point estimates). This demonstrates that significant errors are introduced into Model predictions when the Model is applied without regard for time lagged dependencies (Sec. 3.2.1): Flow standards set using this Model would have to be met for five consecutive years to be consistent with Model assumptions. This problem can be cured by using dynamic regression to accurately model the time-lagged relationships of the Model, as discussed in Section 3.2.

### 3.4. Data Inconsistencies

The periods of record vary from data set to set. The only period common to all data sets is 1969 to 1976. Thus, the regressions for the six equations may capture different relationships due to fundamental changes in the Estuary over time. For example, regressions based on data sets that extend back to 1959 (Delta and Suisun index, loss rate) capture conditions present in the Estuary before the State Water Project pumps came on line in 1968, while those based on post-1969 data (eggs, residual YOY, adult abundance) would not reflect pre-SWP conditions. Likewise, regressions based on data sets that end in 1976 (Delta and Suisun index) fail to capture changes that occurred after the 1977 drought.

Data points for 1966 and 1983 appear to have been inconsistently included or excluded from the various data sets, which could affect the accuracy of predictions made using the Model. For example, 1983 was excluded in developing the Residual YOY equation (Eq. 2, Fig. 1), while 1983 was apparently included in developing the Egg, Loss Rate, and Adult equations (Eqs. 1,6,7, Fig. 1). As another example, the 1966 YOY index was not

[^5]used to develop Equations (2) through (4) (Fig. 1), while an estimate of the 1966 YOY index was used in developing the Adult equation (Eq. 7, Fig. 1).

The use of data sets for different time periods and the use of varying assumptions about 1966 and 1983 raise doubts about the adequacy of the Model for prediction. The relationships among the various variables and equations have shifted since 1959 and the six equations reflect different realities. As discussed in Section 3.5.2, this is compensated for by lumping the majority of the error into a fudge factor referred to as the "residual YOY."

### 3.5. Specification Errors

In addition to the purely statistical flaws that lead to inaccurate predictions, mis-specifying the Model can also cause inaccurate predictions. Specification errors present in the Model include omission of variables, the use of fudge factors, and using the same variable as both the response and predictor variable. Sometimes these problems actually cause collinearity and autocorrelation.
3.5.1 Missing Variables. The Striped Bass Model assumes that the only significant variables affecting the abundance of striped bass are Delta outflow and exports. In WRINT-DWR Exhibit 30, a number of other factors were identified that potentially affect striped bass, including weather phenomena, over-fishing, poaching, pollutants, introduction of exotic species, and agricultural diversions. ${ }^{30}$ One reviewer of the Model also noted that "[w]hile certainly outflow and exports are major factors, they are not the only factors and the model does not appear to recognize anything else, as for example, pesticides and other pollutants, introduced species, changes in environmental conditions (for example, water clarity), or plantings of hatchery raised striped bass. ${ }^{131}$ The CDFG admitted that other factors may also affect bass abundance but felt that "...their impact must be minor for adults to be so well predicted by the model. "32

However, Sections 1 and 2 above demonstrate that the Model does not accurately predict bass abundance when CDFG's analysis are corrected. It is possible that the poor predictions are due,

[^6]in part, to the failure to specify one or more important predictor variables. Additional work is required to explore the influence of non-flow predictor variables on adult abundance.
3.5.2 Fudge Factors. The Delta and Suisun Index equations (Eqs. 3,4, Fig. 1) overpredict the YOY index after 1976 (Fig. 2b, 2e). ${ }^{33}$ To correct for overprediction, CDFG fit a Beverton-Holt relationship to the residuals (actual YOY-predicted YOY) from the Suisun and Delta index regression equations and used it in the Model to predict the YOY index (Fig. 1, Eqs. 2, 4). Of the six regression equations comprising the Striped Bass Model, the residual YOY equation has the poorest coefficient of determination ( $r^{2}=0.41$ ) and the widest confidence intervals (Fig. 2d), and accounts for much of the uncertainty in Model predictions. Absent compelling biological evidence that a stock recruitment or linear relationship between residual YOY and eggs is actually present in the Estuary, the residual yoy equation is nothing more than a fudge factor that contains all of the error associated with the Egg, Delta Index, and Suisun Index equations (Eqs. 1,3,4, Fig. 1).

Several reviewers were not persuaded that a stock recruitment relationship makes sense. Jones \& Stokes pointed out that a stock-recruitment type relationship (e.g., one expressed by an equation of the form $Y=1 /(a+b / X)$ could be due to other changes in the Estuary (e.g., food supply, introduced species) after 1977 and that at any rate, the stock recruitment relationship likely would not have been constant since 1969. 34 Jones \& Stokes' concerns are supported by Cowan ${ }^{35}$ and EA Engineering, Science, and Technology. ${ }^{36}$ Cowan suggests that slight, undetectable changes in survival could have a big impact on the population. EA Engineering points to the need to use agestructured population estimates and age-specific fecundities to directly examine the egg-to-YOY relationship to verify that a stock recruitment relationship actually exists and to determine what portion of the variability is explained by stock recruitment versus environmental variables (rather than assigning 100 percent to stock recruitment). If stock recruitment or some other relationship cannot be verified, the residual yoy should be abandoned since it would have no predictive ability and would be no more than a fudge factor.

[^7]A fudge factor is also applied to the Adult equation "to make predicted values better mimic observed values...n ${ }^{37}$ The factor is 1.08 for an average adult abundance of 1.7 million and 0.936 for an average adult abundance of 1 million. The only justification given for this adjustment is to make the predicted values better fit the measured data. It is well known that a model that is tightly fit using fudge factors is not robust and has limited predictive ability.

### 3.6. Measurement Errors

The difficulty in collecting precise fishery data is well known. Some of these problems are discussed elsewhere. ${ }^{38}$ As several reviewers have pointed out, measurement errors associated with variables in each equation are propagated from one component of the Model to another, contributing to inaccurate predictions. ${ }^{39}$ These are valid concerns, and error propagation is treated in most basic statistic texts on data reduction. ${ }^{40}$ Part of the uncertainty represented by the wide confidence bands shown in Figure 2 and large prediction error shown in Figure 3 is due to measurement errors that have been propagated through the Model.

37 WRINT-DFG-Exhibit 3, p. 39.
38 Donald E. Stevens, Striped Bass (Morone saxatilis)
Monitoring Techniques in the Sacramento-San Joaquin Estuary, In: Proceedings of the Conference on Assessing the Effects of Power-Plant-Induced Mortality on Fish Populations, Webster Van Winkle (Ed.), Pergamon Press, New York, 1977, pp. 91-109; CDFG, Factors Affecting Striped Bass Abundance in the Sacramento-San Joaquin River System, Exhibit 25, 1987; CDFG, Striped Bass Egg and Larval Monitoring, and Effects of Flow Requlation on the Larval Striped Bass Food Chain, in the Sacramento-San Joaquin Estuary, Final Report to SWRCB, May 1988.

39 Orr, November 1, 1991, p. 3, Comment 3; Shaul, November 1, 1991, p. 1.

40 See, for example, Philip R. Bevington, Data Reduction and Error Analysis for the Physical Sciences, McGraw-Hill Book Co., New York, 1969, Chapter 4.

TABLE A-2 (Continued). DAYFLOW

| SEP |  | OCT |  | NOV |  | DEC |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Exp | Out | Exp | Out | Exp | Out | Exp | Out |
|  |  |  |  |  |  |  |  |
| 1937 | 9958 | 1288 | 5683 | 679 | 6016 | 258 | 6938 |
| 2015 | 5500 | 1573 | 5013 | 595 | 13543 | 54 | 19090 |
| 2165 | 5649 | 1440 | 4260 | 684 | 8251 | 253 | 16140 |
| 2141 | 8515 | 1431 | 42900 | 804 | 16351 | 57 | 35013 |
| 2149 | 13480 | 2081 | 14978 | 545 | 27945 | 164 | 22825 |
| 2434 | 9442 | 2269 | 8118 | 746 | 17243 | 61 | 108447 |
| 2072 | 12917 | 1806 | 15091 | 664 | 27350 | 57 | 30136 |
| 2315 | 6905 | 1904 | 6610 | 1026 | 21505 | 501 | 60456 |
| 2634 | 16556 | 1795 | 16749 | 1132 | 16202 | 675 | 20498 |
| 5603 | 6004 | 6249 | 5453 | 5043 | 11120 | 3765 | 25682 |
| 2514 | 20188 | 2006 | 19484 | 1072 | 19964 | 821 | 46190 |
| 3089 | 14587 | 2585 | 13423 | 2031 | 26117 | 1915 | 85369 |
| 3907 | 19659 | 3812 | 13957 | 3047 | 13743 | 2435 | 23967 |
| 6106 | 10476 | 5847 | 11919 | 3309 | 25943 | 3432 | 27133 |
| 5768 | 11153 | 5927 | 14071 | 4903 | 59945 | 3338 | 76406 |
| 5055 | 20981 | 4595 | 18529 | 1949 | 23991 | 2814 | 28017 |
| 7799 | 13419 | 7561 | 16900 | 8010 | 17921 | 7820 | 19953 |
| 8331 | 3670 | 4606 | 3623 | 4244 | 3644 | 2784 | 4213 |
| 1959 | 2791 | 854 | 2075 | 2757 | 4004 | 5983 | 8488 |
| 7487 | 11793 | 5124 | 9633 | 5572 | 10928 | 6051 | 8779 |
| 9262 | 5058 | 7730 | 7821 | 5857 | 12176 | 5973 | 19029 |
| 7683 | 9902 | 6694 | 7368 | 6456 | 6670 | 6763 | 12488 |
| 6797 | 4690 | 5930 | 5218 | 4717 | 35971 | 5166 | 86579 |
| 5284 | 25926 | 5285 | 22986 | 6073 | 39152 | 8428 | 88937 |
| 4203 | 31501 | 2496 | 32293 | 1754 | 74138 | 2142 | 155458 |
| 5498 | 13650 | 5605 | 11916 | 7996 | 25953 | 8464 | 31067 |
| 8719 | 3211 | 7703 | 3378 | 7329 | 6891 | 9858 | 9431 |
| 10490 | 10778 | 7566 | 10628 | 6860 | 7732 | 7260 | 8987 |
| 9070 | 1790 | 5908 | 3789 | 5460 | 4291 | 8986 | 9455 |
| 8119 | 2391 | 5631 | 3226 | 6087 | 6660 | 7184 | 7259 |
| 10753 | 6555 | 10529 | 4926 | 10379 | 5503 | 10442 | 4422 |
| 5918 | 2594 | 3549 | 3498 | 3857 | 4558 | 5205 | 6425 |
| 4235 | 3884 |  |  |  |  |  |  |

TABLE A-2. DAYFLOW
Delta Outflow and Exports - Monthly Means (cfs)

| Delta Outflow and Exports - Monthly Means (cfs) |  |  |  |  |  |  | APR |  | MAY |  | JUN |  | JUL |  | AUG |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JA |  | FE |  | MA |  |  |  |  |  |  |  |  |  |  |  |
| Year | Exp | Out | Exp | Out | Exp | Out | Exp | Out | Exp | Out | Exp | Out | Exp | Out | Exp | Out |
| 1959 | 303 | 32890 | 630 | 58739 | 2023 | 27692 | 2757 | 11607 | 2661 | 7303 | 3564 | 1322 | 4005 | 2561 | 3435 | 5194 |
| 1960 | 255 | 14231 | 630 | 49316 | 2280 | 33273 | 2605 | 16878 | 2688 | 12407 | 3825 | 3847 | 4095 | 2244 | 3556 | 2731 |
| 1961 | 307 | 15580 | 813 | 41997 | 2057 | 28425 | 2900 | 13397 | 2837 | 8580 | 3992 | 3541 | 4656 | 1672 | 3923 | 4007 |
| 1962 | 404 | 11132 | 257 | 74766 | 905 | 47503 | 2761 | 27385 | 2963 | 18173 | 3799 | 10317 | 4229 | 2795 | 3722 | 5028 |
| 1963 | 507 | 20995 | 815 | 103173 | 1823 | 29180 | 1231 | 102776 | 2774 | 53124 | 3543 | 19180 | 4198 | 5639 | 3865 | 5038 |
| 1964 | 577 | 29970 | 1588 | 20915 | 2172 | 13073 | 3065 | 9187 | 3261 | 9784 | 3795 | 5302 | 4619 | 3185 | 4242 | 4704 |
| 1965 | 224 | 135616 | 1561 | 56241 | 2218 | 27860 | 1204 | 56912 | 3193 | 32370 | 3694 | 16190 | 4361 | 5865 | 3904 | 8467 |
| 1966 | 115 | 43464 | 914 | 36316 | 2484 | 24328 | 3108 | 18946 | 3381 | 9835 | 4075 | 2460 | 4597 | 3155 | 4280 | 4846 |
| 1967 | 816 | 62522 | 765 | 84142 | 2002 | 56325 | 1207 | 77685 | 1921 | 74550 | 2162 | 61265 | 2697 | 23864 | 4292 | 9827 |
| 1968 | 1168 | 24257 | 1828 | 52061 | 4487 | 40314 | 5380 | 9932 | 5611 | 6737 | 4708 | 3666 | 5168 | 3684 | 4868 | 5264 |
| 1969 | 7212 | 123140 | 4588 | 159046 | 3123 | 93506 | 2932 | 69375 | 2990 | 64564 | 2214 | 46596 | 3252 | 13143 | 5018 | 12458 |
| 1970 | 1116 | 193121 | 1950 | 111326 | 2265 | 55986 | 4653 | 11027 | 4012 | 10761 | 4997 | 6214 | 5227 | 5256 | 4608 | 7947 |
| 1971 | 1905 | 64152 | 3139 | 34211 | 4702 | 32069 | 4431 | 36983 | 4549 | 26406 | 5768 | 21218 | 6509 | 11654 | 6701 | 12988 |
| 1972 | 1615 | 21339 | 3731 | 21968 | 6682 | 18078 | 6356 | 7542 | 6495 | 5140 | 8111 | 2891 | 5001 | 6211 | 6072 | 6470 |
| 1973 | 2962 | 101685 | 1178 | 102165 | 1282 | 76907 | 3352 | 22191 | 6501 | 11699 | 7355 | 7211 | 7693 | 4599 | 7774 | 5963 |
| 1974 | 1974 | 138699 | 5455 | 59178 | 6275 | 77575 | 4203 | 109547 | 7130 | 25544 | 9130 | 16943 | 10691 | 9365 | 9474 | 12783 |
| 1975 | 5472 | 17489 | 6717 | 57330 | 6079 | 66834 | 6304 | 34519 | 5583 | 28796 | 4520 | 22508 | 5184 | 11129 | 8988 | 9523 |
| 1976 | 8260 | 9346 | 7793 | 7495 | 8351 | 7858 | 5037 | 8833 | 5488 | 4066 | 4152 | 3915 | 4109 | 4343 | 6836 | 4509 |
| 1977 | 7042 | 4365 | 4335 | 4924 | 3813 | 3070 | 1295 | 3083 | 2987 | 3999 | 739 | 2521 | 845 | 3212 | 1529 | 2514 |
| 1978 | 9886 | 66171 | 10309 | 56159 | 5919 | 85544 | 3271 | 61276 | 3058 | 40874 | 7621 | 9086 | 8088 | 3974 | 8425 | 5927 |
| 1979 | 4104 | 30522 | 2939 | 46341 | 4348 | 38086 | 5882 | 14485 | 6245 | 13435 | 6341 | 5326 | 9339 | 5384 | 10362 | 3475 |
| 1980 | 6377 | 118212 | 6185 | 121653 | 4341 | 99171 | 5343 | 28689 | 4630 | 20912 | 5961 | 14870 | 6869 | 11.191 | 9212 | 4253 |
| 1981 | 8264 | 18326 | 7239 | 21174 | 4834 | 26467 | 8090 | 11653 | 4478 | 9143 | 4032 | 4596 | 7046 | 5296 | 9315 | 3161 |
| 1982 | 5176 | 97706 | 9452 | 88727 | 10417 | 80089 | 9603 | 142203 | 5994 | 57876 | 3935 | 28515 | 4032 | 16849 | 8096 | 13438 |
| 1983 | 10085 | 89755 | 10246 | 175757 | 5371 | 266688 | 3814 | 118109 | 3293 | 98707 | 5010 | 71038 | 5207 | 43860 | 7190 | 24567 |
| 1984 | 1720 | 100906 | 5767 | 41515 | 6916 | 34929 | 7685 | 14732 | 5929 | 11204 | 6165 | 8038 | 9457 | 10252 | 9515 | 8272 |
| 1985 | 5835 | 15120 | 7614 | 15590 | 8616 | 10432 | 7342 | 6913 | 6215 | 7378 | 6530 | 5215 | 9465 | 4934 | 10111 | 2325 |
| 1986 | 9070 | 15209 | 9821 | 205414 | 2231 | 169448 | 3273 | 46572 | 5361 | 15911 | 6076 | 9322 | 8607 | 7384 | 9951 | 5135 |
| 1987 | 6251 | 10819 | 6845 | 16859 | 5600 | 22916 | 7021 | 6291 | 5313 | 4951 | 5183 | 3496 | 8952 | 3829 | 9800 | 2851 |
| 1988 | 10418 | 19593 | 10023 | 3045 | 8441 | 4542 | 8570 | 11499 | 6263 | 4747 | 5900 | 3197 | 7967 | 3920 | 8794 | 2472 |
| 1989 | 10194 | 3635 | 8201 | 6405 | 10261 | 38951 | 10447 | 11808 | 6220 | 7531 | 5271 | 6317 | 9515 | 6357 | 11319 | 4634 |
| 1990 | 10621 | 9913 | 10553 | 6815 | 10558 | 3906 | 9667 | 6041 | 3391 | 7837 | 3492 | 4999 | 6245 | 4115 | 6676 | 4612 |
| 1991 | . 4912 | 4013 | 4521 | 7420 | 9763 | 24626 | 7499 | 3787 | 2685 | 3998 | 1925 | 4169 | 2574 | 3479 | 3818 | 2696 |

TABLE A-1. DATA USED TO DEVELOP STRIPED BASS MODEL

| Year | Eggs | Adults (wild) | Adults (w/ hatchery) | Sulsun | Delta | YOY | Export <br> Losses | Aprajul Outflow | Apr-Jul Exports | Apr-Jul Diversn | Aug-Mar Exports | Aug-Dec Outflow |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1959 |  |  |  | 3 | 30.7 | 33.7 | 1,668,181 | 5,698 | 3,247 | 6,350 | 1,345 | 6,758 |
| 1960 |  |  |  | 13.6 | 32.0 | 45.6 | 2,414,048 | 8,844 | 3,303 | 6,407 | 1,371 | 9,175 |
| 1961 |  |  |  | 6.4 | 25.2 | 31.6 | 2,989,860 | 6,798 | 3,596 | 6,700 | 1,254 | 7,661 |
| 1962 |  |  |  | 32.1 | 46.8 | 78.9 | 2,694,309 | 14,668 | 3,438 | 6,541 | 1,413 | 21,561 |
| 1963 |  |  |  | 43.5 | 38.2 | 81.7 | 1,909,488 | 45,180 | 2,937 | 6,040 | 1,643 | 16,853 |
| 1964 |  |  |  | 20.7 | 54.7 | 75.4 | 834,137 | 6,865 | 3,685 | 6,788 | 1,719 | 29,591 |
| 1965 |  |  |  | 67.8 | 49.4 | 117.2 | 2,149,306 | 27,834 | 3,113 | 6,216 | 1,502 | 18,792 |
| 1966 |  |  |  |  |  |  | 4,811,106 | 8,599 | 3,790 | 6,894 | 1,701 | 20,064 |
| 1967 |  |  |  | 73.6 | 35.1 | 108.7 | 2,220,430 | 59,341 | 1,997 | 5,100 | 2,251 | 15,966 |
| 1968 |  |  |  | 17.7 | 39.6 | 57.3 | 4,473,927 | 6,005 | 5,217 | 8,320 | 5,056 | 10,705 |
| 1969 | 319.1 | 1,646,026 | 1,646,026 | 40.2 | 33.6 | 73.8 | 2,360,665 | 48,420 | 2,847 | 5,950 | 2,095 | 23,657 |
| 1970 | 267.2 | 1,727,394 | 1,727,394 | 41.9 | 36.6 | 78.5 | 10,053,728 | 8,315 | 4,722 | 7,826 | 2,997 | 29,489 |
| 1971 | 255.7 | 1,599,715 | 1,599,715 | 45 | 24.6 | 69.6 | 9,185,289 | 24,065 | 5,314 | 8,418 | 3,991 | 16,863 |
| 1972 | 265.3 | 1,882,907 | 1,882,907 | 21.1 | 13.4 | 34.5 | 3,568,058 | 5,446 | 6,491 | 9,594 | 3,774 | 16,388 |
| 1973 | 354.2 | 1,637,159 | 1,637,159 | 47.1 | 15.6 | 62.7 | 11,176,662 | 11,425 | 6,225 | 9,329 | 5,177 | 33,508 |
| 1974 | 300.5 | 1,477,213 | 1,477,213 | 63.4 | 17.4 | 80.8 | 21,807,197 | 40,350 | 7,789 | 10,892 | 5,269 | 20,860 |
| 1975 | 434.2 | 1,849,770 | 1,849,770 | 42.1 | 23.4 | 65.5 | 18,620,410 | 24,238 | 5,398 | 8,501 | 8,073 | 15,543 |
| 1976 | 269.0 | 1,581,076 | 1,581,076 | 14.8 | 21.1 | 35.9 | 3,615,048 | 5,289 | 4,697 | 7,800 | 5,249 | 3,932 |
| 1977 | 231.4 | 924,301 | 924,301 | 0.7 | 8.3 | 9 | 1,428,579 | 3,204 | 1,467 | 4,570 | 4,900 | 3,974 |
| 1978 | 129.6 | 1,151,642 | 1,151,642 | 13.1 | 16.5 | 29.6 | 2,798,063 | 28,803 | 5,510 | 8,613 | 5,506 | 9,412 |
| 1979 | 90.3 | 1,155,701 | 1,155,701 | 11.5 | 5.4 | 16.9 | 2,746,237 | 9,658 | 6,952 | 10,055 | 7,011 | 9,512 |
| 1980 | 125.7 | 1,115,999 | 1,115,999 | 11.2 | 2.8 | 14 | 2,853,551 | 18,916 | 5,701 | 8,804 | 7,143 | 8,136 |
| 1981 | 99.9 | 911,300 | 911,300 | 13.7 | 15.4 | 29.1 | 2,536,186 | 7,672 | 5,912 | 9,015 | 7,121 | 27,124 |
| 1982 | 68.5 | 825,126 | 825,126 | 39.2 | 9.5 | 48.7 | 2,820,971 | 61,361 | 5,891 | 8,994 | 7,359 | 38,088 |
| 1983 | 121.8 | 1,009,748 | 1,009,748 |  |  | 15.4 | 182,129 | 82,929 | 4,331 | 7,434 | 4,024 | 63,591 |
| 1984 | 77.1 | 1,042,668 | 1,048,244 | 20 | 6.3 | 26.3 | 6,486,207 | 11,057 | 7,309 | 10,412 | 7,393 | 18,172 |
| 1985 | 97.9 | 1,024,188 | 1,038,126 | 4.1 | 2.2 | 6.3 | 3,909,444 | 6,110 | 7,388 | 10,491 | 8,105 | 5,047 |
| 1986 | 165.2 | 1,037,127 | 1,064,142 | 41.1 | 23.8 | 64.9 | 19,221,607 | 19,797 | 5,829 | 8,933 | 7,603 | 8,652 |
| 1987 | 176.1 | 998,349 | 1,037,617 | 5.3 | 7.3 | 12.6 | 14,031,947 | 4,642 | 6,617 | 9,721 | 8,513 | 4,435 |
| 1988 | 176.4 | 903,899 | 980,068 | 0.7 | 3.9 | 4.6 | 1,949,138 | 5,841 | 7,175 | 10,278 | 8,059 | 4,402 |
| 1989 | 103.5 | 786,380 | 911,745 | 2.0 | 3.1 | 5.1 | 6,092,415 | 8,003 | 7,863 | 10,967 | 10,644 | 5,208 |
| 1990 | 91.6 | 591,241 | 679,376 | 1.5 | 2.8 | 4.3 |  | 5,748 | 5,699 | 8,802 | 5,550 | 4,337 |
| 1991 | 160.2 | 961,063 | 1,161,071 | 1.6 | 3.9 | 5.5 |  | 3,858 | 3,671 | 6,774 |  |  |

## APPENDIX A

DATA USED TO DEVELOP THE STRIPED BASS MODEL


[^0]:    7 Dick R. Wittink, The Application of Regression Analysis, Allyn and Bacon, Inc., Boston, 1988, p. 267-268.

[^1]:    14 Letter from Harold K. Chadwick, CDFG, to Leo Winternitz, SWRCB, Re: Department of Fish and Game Responses to Comments on the Striped Bass Model and Additional Analyses, November 21, 1991, p. 3, Comment 6.

[^2]:    15 Wittink, 1988, p. 83-90.
    ${ }^{16}$ Samprit Chatterjee and Bertram Price, Regression Analysis By Example, 2nd Edition, John Wiley \& Sons, Inc., New York, 1991, p. 174 .

[^3]:    20 Willits, March 29, 1992, p. 2-3.

[^4]:    21 Alan Pankratz, Forecasting with Dynamic Regression Models, John Wiley \& Sons, Inc., New York, 1991, p. 8-15.

[^5]:    28 WRINT-DFG Exhibit 3, p. 39, 41.
    29 Hanson, November 7, 1991, p. 4.

[^6]:    30 Randall Brown, Bay/Delta Fish Resources, WRINT-DWR Exhibit 30, July 1992.

    31 Patterson, November 21, 1991, p. 2, Comment 6.
    32 Letter from H.K. Chadwick, CDFG, to Roger K. Patterson, Bureau of Reclamation, Re: Responses to Comments on Striped Bass Model, November 22, 1991, p. 2, Comment 6.

[^7]:    33 WRINT-DFG-Exhibit 3, p. 27 and Figure 7.
    34 Shaul, November 1, 1991, p. 1.
    35 Cowan, January 7, 1992, p. 3.
    36 Orr, November 1, 1991, p. 2, Comment 1.

